

Mark Scheme (Results)

January 2012

GCE Further Pure FP1 (6667) Paper 01

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General Marking Guidance

- All candidates must receive the same treatment. Examiners must mark the first candidate in exactly the same way as they mark the last.
- Mark schemes should be applied positively. Candidates must be rewarded for what they have shown they can do rather than penalised for omissions.
- Examiners should mark according to the mark scheme not according to their perception of where the grade boundaries may lie.
- There is no ceiling on achievement. All marks on the mark scheme should be used appropriately.
- All the marks on the mark scheme are designed to be awarded. Examiners should always award full marks if deserved, i.e. if the answer matches the mark scheme. Examiners should also be prepared to award zero marks if the candidate's response is not worthy of credit according to the mark scheme.
- Where some judgement is required, mark schemes will provide the principles by which marks will be awarded and exemplification may be limited.
- When examiners are in doubt regarding the application of the mark scheme to a candidate's response, the team leader must be consulted.
- Crossed out work should be marked UNLESS the candidate has replaced it with an alternative response.

EDEXCEL GCE MATHEMATICS

General Instructions for Marking

- 1. The total number of marks for the paper is 75.
- 2. The Edexcel Mathematics mark schemes use the following types of marks:
- M marks: method marks are awarded for 'knowing a method and attempting to apply it', unless otherwise indicated.
- A marks: Accuracy marks can only be awarded if the relevant method (M) marks have been earned.
- **B** marks are unconditional accuracy marks (independent of M marks)
- Marks should not be subdivided.
- 3. Abbreviations

These are some of the traditional marking abbreviations that will appear in the mark schemes and can be used if you are using the annotation facility on ePEN.

- bod benefit of doubt
- ft follow through
- the symbol / will be used for correct ft
- cao correct answer only
- cso correct solution only. There must be no errors in this part of the question to obtain this mark
- isw ignore subsequent working
- awrt answers which round to
- SC: special case
- oe or equivalent (and appropriate)
- dep dependent
- indep independent
- dp decimal places
- sf significant figures
- * The answer is printed on the paper
- 4. All A marks are 'correct answer only' (cao.), unless shown, for example, as A1 ft to indicate that previous wrong working is to be followed through. After a misread however, the subsequent A marks affected are treated as A ft, but manifestly absurd answers should never be awarded A marks.

General Principals for Core Mathematics Marking

(But note that specific mark schemes may sometimes override these general principles).

Method mark for solving 3 term quadratic:

1. Factorisation

$$(x^2 + bx + c) = (x + p)(x + q), \text{ where } |pq| = |c|, \text{ leading to } x = \dots$$

$$(ax^2 + bx + c) = (mx + p)(nx + q), \text{ where } |pq| = |c| \text{ and } |mn| = |a|, \text{ leading to } x = \dots$$

2. Formula

Attempt to use <u>correct</u> formula (with values for a, b and c), leading to x = ...

3. Completing the square

Solving
$$x^2 + bx + c = 0$$
: $\left(x \pm \frac{b}{2}\right)^2 \pm q \pm c$, $q \neq 0$, leading to $x = ...$

Method marks for differentiation and integration:

1. <u>Differentiation</u>

Power of at least one term decreased by 1. $(x^n \rightarrow x^{n-1})$

2. Integration

Power of at least one term increased by 1. $(x^n \rightarrow x^{n+1})$

Use of a formula

Where a method involves using a formula that has been learnt, the advice given in recent examiners' reports is that the formula should be quoted first.

Normal marking procedure is as follows:

<u>Method mark</u> for quoting a correct formula and attempting to use it, even if there are mistakes in the substitution of values.

Where the formula is <u>not</u> quoted, the method mark can be gained by implication from <u>correct</u> working with values, but may be lost if there is any mistake in the working.

January 2012 6667 Further Pure Mathematics FP1 Mark Scheme

Question Number	Scheme	Notes	Marks
1(a)	$\arg z_1 = -\arctan(1)$	-arctan(1) or arctan(-1)	M1
	$=-\frac{\pi}{4}$	or -45 or awrt -0.785 (oe e.g $\frac{7\pi}{4}$)	A1
	Correct an	nswer only 2/2	(2)
(b)	$z_1 z_2 = (1-i)(3+4i) = 3-3i+4i-4i^2$	At least 3 correct terms (Unsimplified)	M1
	=7+i	cao	A1
			(2)
(c)	$\frac{z_2}{z_1} = \frac{(3+4i)}{(1-i)} = \frac{(3+4i).(1+i)}{(1-i).(1+i)}$	Multiply top and bottom by (1 + i)	M1
	$= \frac{(3+4i).(1+i)}{2}$ $= -\frac{1}{2} + \frac{7}{2}i$	(1+i)(1-i)=2	A1
	$=-\frac{1}{2}+\frac{7}{2}i$	or $\frac{-1+7i}{2}$	A1
	Special case $\frac{z_1}{z_2} = \frac{(1-i)}{(3+4i)} = \frac{(1-i).(3-4i)}{(3+4i).(3-4i)}$ Allow M1A0A0		
			(3)
	Correct answers only in (b) and (c) scores no marks		

$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	Question Number	Scheme	Notes	Marks
	2	$f(x) = x^4 + x - 1$		
	(a)	10	Either any one of $f(0.5) = awrt - 0.4$ or $f(1) = 1$	M1
$f(0.625) = -0.222412109375(-\frac{911}{4096}) \qquad f(0.75) = \text{awrt } 0.07 \text{ and } f(0.625) = \text{awrt } -0.2 \qquad \text{A1}$ $0.625 \text{,, } \alpha \text{,, } 0.75 \qquad 0.625 \text{, } \alpha \text{,, } 0.75 \text{ or } [0.625, 0.75] \text{ or }$		Sign change (positive, negative) (and $f(x)$ is continuous) therefore (a root) α is between		A1
$f(0.625) = -0.222412109375(-\frac{911}{4096}) \qquad f(0.75) = \text{awrt } 0.07 \text{ and } f(0.625) = \text{awrt } -0.2 \qquad \text{A1}$ $0.625 \text{,, } \alpha \text{,, } 0.75 \qquad 0.75 \text{ or } [0.625, 0.75] \text{ or } [0.625, 0.75] \text{ or } [0.625, 0.75]. \qquad \text{A1}$ $0.625 \text{,, } \alpha \text{,, } 0.75 \qquad \text{or } [0.625, 0.75] \text{ or } (0.625, 0.75). \qquad \text{A1}$ $0.625 \text{,, } \alpha \text{,, } 0.75 \qquad \text{or } [0.625, 0.75] \text{ or } (0.625, 0.75). \qquad \text{A1}$ $0.625 \text{,, } \alpha \text{,, } 0.75 \qquad \text{or } [0.625, 0.75] \text{ or } (0.625, 0.75). \qquad \text{A1}$ $0.625 \text{,, } \alpha \text{,, } 0.75 \qquad \text{or } [0.625, 0.75] \text{ or } (0.625, 0.75). \qquad \text{A1}$ $0.625 \text{,, } \alpha \text{,, } 0.75 \qquad \text{or } [0.625, 0.75] \text{ or } (0.625, 0.75). \qquad \text{A1}$ $0.625 \text{,, } \alpha \text{,, } 0.75 \qquad \text{or } [0.625, 0.75] \text{ or } (0.625, 0.75). \qquad \text{A1}$ $0.625 \text{,, } \alpha \text{,, } 0.75 \qquad \text{or } [0.625, 0.75] \text{ or } (0.625, 0.75). \qquad \text{A1}$ $0.625 \text{,, } \alpha \text{,, } 0.75 \qquad \text{or } [0.625, 0.75] \text{ or } (0.625, 0.75). \qquad \text{A1}$ $0.625 \text{,, } \alpha \text{,, } 0.75 \qquad \text{or } [0.625, 0.75] \text{ or } (0.625, 0.75). \qquad \text{A1}$ $0.625 \text{,, } \alpha \text{,, } 0.75 \qquad \text{or } [0.625, 0.75] \text{ or } (0.625, 0.75). \qquad \text{A1}$ $0.625 \text{,, } \alpha \text{,, } 0.75 \qquad \text{or } [0.625, 0.75] \text{ or } (0.625, 0.75). \qquad \text{A1}$ $0.625 \text{,, } \alpha \text{,, } 0.75 \qquad \text{or } [0.625, 0.75] \text{ or } (0.625, 0.75). \qquad \text{A1}$ $0.625 \text{,, } \alpha \text{,, } 0.75 \qquad \text{or } [0.625, 0.75] \text{ or } (0.625, 0.75). \qquad \text{A1}$ $0.625 \text{,, } \alpha \text{,, } 0.75 \qquad \text{or } [0.625, 0.75] \text{ or } (0.625, 0.75). \qquad \text{A1}$ $0.625 \text{,, } \alpha \text{,, } 0.75 \qquad \text{or } [0.625, 0.75] \text{ or } (0.625, 0.75). \qquad \text{A1}$ $0.625 \text{,, } \alpha \text{,, } 0.75 \qquad \text{or } [0.625, 0.75] \text{ or } (0.625, 0.75). \qquad \text{A1}$ $0.625 \text{,, } \alpha \text{,, } 0.75 \qquad \text{or } [0.625, 0.75] \text{ or } [0.625, 0.75]. \qquad \text{A1}$ $0.625 \text{,, } \alpha \text{,, } 0.75 \qquad \text{or } [0.625, 0.75]. \qquad \text{A2}$ $0.625 \text{,, } \alpha \text{,, } 0.75 \qquad \text{or } [0.625, 0.75]. \qquad \text{A2}$ $0.625 \text{,, } \alpha \text{,, } 0.75 \qquad \text{or } [0.625, 0.75]. \qquad \text{A2}$ $0.625 \text{,, } \alpha \text{,, } 0.75 \qquad \text{or } [0.625, 0.75]. \qquad \text{A2}$ $0.625 \text{,, } \alpha \text{,, } 0.75 \qquad \text{or } [0.625, 0.75]. \qquad \text{A2}$ $0.625 \text{,, } \alpha $				(2)
$f(0.625) = -0.222412109375(-\frac{911}{4096}) \qquad f(0.75) = \text{awrt } 0.07 \text{ and } f(0.625) = \text{awrt } -0.2 \qquad \text{A1}$ $0.625 \text{, } \alpha \text{, } 0.75 \qquad 0.625 \text{, } \alpha \text{, } 0.75 \text{ or } [0.625, 0.75] \text{ or } [0$	(b)	$f(0.75) = 0.06640625(\frac{17}{256})$	Attempt f(0.75)	M1
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$		$f(0.625) = -0.222412109375(-\frac{911}{4096})$	$f(0.75) = awrt \ 0.07 \ and \ f(0.625) = awrt \ -0.2$	A1
or equivalent in words. In (b) there is no credit for linear interpolation and a correct answer with no working scores no marks. (c) $f'(x) = 4x^3 + 1$ $x_1 = 0.75$ $x_2 = 0.75 - \frac{f(0.75)}{f'(0.75)} = 0.75 - \frac{0.06640625}{2.6875(43/16)}$ Attempt Newton-Raphson $x_2 = 0.72529(06976) = \frac{499}{688}$ Correct first application – a correct numerical expression e.g. $0.75 - \frac{17/256}{43/16}$ A1 or awrt 0.725 (may be implied) $x_3 = 0.724493\left(\frac{499}{688} - \frac{0.002015718978}{2.562146811}\right)$ Awrt 0.724 A1 $(\alpha) = 0.724$ A1			0.625 ,, α ,, 0.75 or $0.625 < \alpha < 0.75$	
		$0.625, \alpha, 0.75$	or [0.625, 0.75] or (0.625, 0.75).	A1
correct answer with no working scores no marks. (c) $f'(x) = 4x^3 + 1$ $x_1 = 0.75$ $x_2 = 0.75 - \frac{f(0.75)}{f'(0.75)} = 0.75 - \frac{0.06640625}{2.6875(43/16)}$ Attempt Newton-Raphson $x_2 = 0.72529(06976) = \frac{499}{688}$ Correct first application – a correct numerical expression e.g. $0.75 - \frac{17/256}{43/16}$ or awrt 0.725 (may be implied) $x_3 = 0.724493 \left(\frac{499}{688} - \frac{0.002015718978}{2.562146811}\right)$ Awrt 0.724 A1 $(\alpha) = 0.724$ Cao			•	
(c) $ f'(x) = 4x^3 + 1 $ Correct derivative (May be implied later by e.g. $4(0.75)^3 + 1$) B1 $ x_1 = 0.75 $ Attempt Newton-Raphson M1 $ x_2 = 0.72529(06976) = \frac{499}{688} $ Correct first application – a correct numerical expression e.g. $0.75 - \frac{17/256}{43/16}$ A1 $ x_3 = 0.724493 \left(\frac{499}{688} - \frac{0.002015718978}{2.562146811} \right) $ Awrt 0.724 A1 $ (\alpha) = 0.724 $ Cao A1			_	(3)
by e.g. $4(0.75)^3 + 1$ by e.	(c)			
$x_2 = 0.75 - \frac{f(0.75)}{f'(0.75)} = 0.75 - \frac{0.06640625}{2.6875(43/16)}$ Attempt Newton-Raphson M1 $x_2 = 0.72529(06976) = \frac{499}{688}$ Correct first application – a correct numerical expression e.g. $0.75 - \frac{17/256}{43/16}$ A1 or awrt 0.725 (may be implied) $x_3 = 0.724493\left(\frac{499}{688} - \frac{0.002015718978}{2.562146811}\right)$ Awrt 0.724 A1 $(\alpha) = 0.724$ cao A1	(-)	$f'(x) = 4x^3 + 1$		B1
Correct first application – a correct numerical expression e.g. $0.75 - \frac{17}{256}$ A1 or awrt 0.725 (may be implied) $x_3 = 0.724493 \left(\frac{499}{688} - \frac{0.002015718978}{2.562146811} \right) \text{Awrt } 0.724 \qquad \qquad \text{A1}$ $(\alpha) = 0.724 \qquad \qquad \text{cao} \qquad \qquad \text{A1}$		$x_1 = 0.75$		
$x_2 = 0.72529(06976) = \frac{499}{688}$ numerical expression e.g. $0.75 - \frac{17/256}{43/16}$ or awrt 0.725 (may be implied) $x_3 = 0.724493 \left(\frac{499}{688} - \frac{0.002015718978}{2.562146811} \right)$ Awrt 0.724 $(\alpha) = 0.724$ cao A1		$x_2 = 0.75 - \frac{f(0.75)}{f'(0.75)} = 0.75 - \frac{0.06640625}{2.6875(43/16)}$	Attempt Newton-Raphson	M1
or awrt 0.725 (may be implied) $x_3 = 0.724493 \left(\frac{499}{688} - \frac{0.002015718978}{2.562146811} \right) \qquad \text{Awrt 0.724} \qquad \qquad \text{A1}$ $(\alpha) = 0.724 \qquad \qquad \text{cao} \qquad \qquad \text{A1}$			Correct first application – a correct	
or awrt 0.725 (may be implied) $x_3 = 0.724493 \left(\frac{499}{688} - \frac{0.002015718978}{2.562146811} \right) \qquad \text{Awrt 0.724}$ $(\alpha) = 0.724 \qquad \text{cao} \qquad \text{A1}$		$x_2 = 0.72529(06976) = \frac{499}{688}$	numerical expression e.g. $0.75 - \frac{17/256}{43/16}$	A1
$x_3 = 0.724493 \left(\frac{1}{688} - \frac{1}{2.562146811} \right)$ Awrt 0.724 A1 $(\alpha) = 0.724$ cao A1				
		$ x_2 = 0.724493 $	Awrt 0.724	A1
		$(\alpha) = 0.724$	cao	A1
		A final answer of 0.724 with evidence of NR applied twice with no incorrect work should score 5/5		
		OLI DIIOGIA DOULO DIO		Total 10

Question Number	Scheme	Notes	Marks
3(a)	Focus (4,0)		
	D: 4: 4 0	x + ``4'' = 0 or x = -``4''	M1
	Directrix $x+4=0$	x + 4 = 0 or $x = -4$	A1
			(3)
(b)	$y = 4x^{\frac{1}{2}} \Rightarrow \frac{\mathrm{d}y}{\mathrm{d}x} = 2x^{-\frac{1}{2}}$	$\frac{\mathrm{d}y}{\mathrm{d}x} = k x^{-\frac{1}{2}}$	
	$y^{2} = 16x \Rightarrow 2y \frac{dy}{dx} = 16$ or $\frac{dy}{dx} = \frac{dy}{dt} \cdot \frac{dt}{dx} = 8 \cdot \frac{1}{8t}$	$ky \frac{dy}{dx} = c$ their $\frac{dy}{dt} \times \left(\frac{1}{\text{their } \frac{dx}{dt}}\right)$	M1
	$\frac{dy}{dx} = 2x^{-\frac{1}{2}} \text{ or } 2y \frac{dy}{dx} = 16 \text{ or } \frac{dy}{dx} = 8.\frac{1}{8t}$	Correct differentiation	A1
	At P , gradient of normal = $-t$	Correct normal gradient with no errors seen.	A1
	$y - 8t = -t(x - 4t^2)$	Applies $y - 8t = \text{their } m_N (x - 4t^2)$ or $y = (\text{their } m_N)x + c$ using $x = 4t^2$ and $y = 8t$ in an attempt to find c. Their m_N must be different from their m_T and must be a function of t .	M1
	$y + tx = 8t + 4t^3 *$	cso **given answer**	A1
	Special case – if the correct gradient is <u>quoted</u> could score M0A0A0M1A1		
			Total 8

Question Number	Scheme	Notes	Marks
4(a)	$ \begin{pmatrix} 0 & 1 \\ 1 & 0 \end{pmatrix} \begin{pmatrix} 1 & 2 & 2 \\ 1 & 1 & 4 \end{pmatrix} = \begin{pmatrix} 1 & 1 & 4 \\ 1 & 2 & 2 \end{pmatrix} $	Attempt to multiply the right way round with at least 4 correct elements	M1
	T'has coordinates (1,1), (1,2) and (4,2) or $\begin{pmatrix} 1 \\ 1 \end{pmatrix}$, $\begin{pmatrix} 4 \\ 2 \end{pmatrix}$ NOT just $\begin{pmatrix} 1 \\ 1 \end{pmatrix}$ $\begin{pmatrix} 4 \\ 2 \end{pmatrix}$ 2	Correct coordinates or vectors	A1
4.)			(2)
(b)	75 (9) 41 · 1 · 1	Reflection	B1
	Reflection in the line $y = x$	y = x	B1
	Allow 'in the axis' 'about the line' $y = x$ etc. Provided both reference to the origin unless there is a c		
			(2)
(c)	(4 2)(1 2) (2 0)	2 correct elements	(2) M1
	$\mathbf{QR} = \begin{pmatrix} 4 & -2 \\ 3 & -1 \end{pmatrix} \begin{pmatrix} 1 & 2 \\ 3 & 4 \end{pmatrix} = \begin{pmatrix} -2 & 0 \\ 0 & 2 \end{pmatrix}$	Correct matrix	A1
	Note that $\mathbf{RQ} = \begin{pmatrix} 1 & 2 \\ 3 & 4 \end{pmatrix} \begin{pmatrix} 4 & -2 \\ 3 & -1 \end{pmatrix} = \begin{pmatrix} 10 \\ 24 \end{pmatrix}$	$\begin{pmatrix} -4 \\ -10 \end{pmatrix}$ scores M0A0 in (c) but	
	allow all the marks in (d) and (e)		
			(2)
(d)	$\det\left(\mathbf{QR}\right) = -2 \times 2 - 0 = -4$	"-2"x"2" – "0"x"0"	M1
		-4	A1
	Answer only scores 2/	/2	(2)
	1		
	$\overline{\det(\mathbf{Q}\mathbf{R})}$ scores Mo	0	
(e)	Area of $T = \frac{1}{2} \times 1 \times 3 = \frac{3}{2}$	Correct area for T	B1
		Attempt at " $\frac{3}{2}$ "×±"4"	M1
	Area of $T'' = \frac{3}{2} \times 4 = 6$	6 or follow through their det(QR) x Their triangle area provided area > 0	A1ft
			(3)
			Total 11

Question Number	Scheme	Notes	Marks
5(a)	$(z_2) = 3 - i$		B1
	$(z - (3+i))(z - (3-i)) = z^2 - 6z + 10$	Attempt to expand $(z - (3+i))(z - (3-i))$ or any valid method to establish the quadratic factor e.g. $z = 3 \pm i \Rightarrow z - 3 = \pm i \Rightarrow z^2 - 6z + 9 = -1$ $z = 3 \pm \sqrt{-1} = \frac{6 \pm \sqrt{-4}}{2} \Rightarrow b = -6, c = 10$ Sum of roots 6, product of roots 10 $\therefore z^2 - 6z + 10$	M1
	$(z^2 - 6z + 10)(z - 2) = 0$	Attempt at linear factor with their cd in $(z^2 + az + c)(z + d) = \pm 20$ Or $(z^2 - 6z + 10)(z + a) \Rightarrow 10a = -20$ Or attempts f(2)	M1
	$(z_3) = 2$		A1
	Showing that $f(2) = 0$ is equivalent to s 4 marks quite easily e.g. $z_2 = 3 - i$ B1, Answers only can score 4/4	scoring both M's so it is possible to gain all shows $f(2) = 0$ M2, $z_3 = 2$ A1.	(4)
5(b)	First B1 for plotting (3, 1) and (3, -1) correctly with an indication of scale or labelled with coordinates (allow points/lines/crosses/vectors etc.) Allow <i>i/-i</i> for 1/-1 marked on imaginary axis. Second B1 for plotting (2, 0) correctly relative to the conjugate pair with an indication of scale or labelled with coordinates or just 2		
			Tota l 6

Question Number	Scheme Notes		Marks	
6(a)	$n = 1$, LHS = $1^3 = 1$, RHS = $\frac{1}{4} \times 1^2 \times 2^2 = 1$	Shows both LHS = 1 and RHS = 1		B1
	Assume true for $n = k$			
	When n = k + 1 $\sum_{r=1}^{k+1} r^3 = \frac{1}{4}k^2(k+1)^2 + (k+1)^3$	Adds $(k+1)^3$ to t	he given result	M1
	1	Attempt to factor	•	dM1
	$= \frac{1}{4}(k+1)^2[k^2+4(k+1)]$	Correct expression $\frac{1}{4}(k+1)^2$ factoris		A1
	$= \frac{1}{4}(k+1)^{2}(k+2)^{2}$ Must see 4 things: <u>true for n = 1</u> , <u>assumption true for n = k</u> , <u>said true for</u>	Fully complete proof with no errors and comment. All the previous marks must have been scored.		Alcso
	$\underline{n = k + 1}$ and therefore <u>true for all n</u>			
	See extra notes for alternative approaches			(5)
(b)	$\sum (r^3 - 2) = \sum r^3 - \sum 2$	Attempt two sum	S	M1
	$\sum r^3 - \sum 2n \text{ is M0}$			
	$= \frac{1}{4} n^2 (n+1)^2 - 2n$	Correct expression		A1
	$= \frac{n}{4}(n^3 + 2n^2 + n - 8) *$	Completion to printed answer with no errors seen.		A1
				(3)
(c)	$\sum_{r=20}^{r=50} (r^3 - 2) = \frac{50}{4} \times 130042 - \frac{19}{4} \times 7592$	Attempt $S_{50} - S_{20}$ or $S_{50} - S_{19}$ and substitutes into a correct expression at least once. Correct numerical expression (unsimplified)		M1
	(=1625525 - 36062)			A1
	= 1 589 463			A1
			T	(3)
(c) Way 2	$\sum_{r=20}^{r=50} (r^3 - 2) = \sum_{r=20}^{r=50} r^3 - \sum_{r=20}^{r=50} (2) = \frac{50^2}{4} \times 51^2 - \frac{1}{12} \times \frac{1}{12} = \frac{1}{12} \times \frac{1}{$	$-\frac{19^2}{4} \times 20^2 - 2 \times 31$	$\begin{array}{c} M1 \text{ for } (S_{50}-S_{20} \text{ or } S_{50}\\ -S_{19} \text{ for cubes}) - (2x30\\ \text{ or } 2x31) \\ \hline A1 \text{ correct numerical}\\ \text{ expression} \end{array}$	Total 11
	=1 589 463		A1	

Question Number	Scheme	Notes	Marks
7(a)	$u_2 = 3, \ u_3 = 7$		B1, B1
			(2)
(b)	At $n = 1$, $u_1 = 2^1 - 1 = 1$ and so result true for $n = 1$		B1
	Assume true for $n = k$; $u_k = 2^k - 1$		
	and so $(2n+1) \cdot 2(2^k+1) + 1$	Substitutes u_k into u_{k+1} (must see this line)	M1
	and so $u_{k+1} (= 2u_k + 1) = 2(2^k - 1) + 1$	Correct expression	A1
	$u_{k+1} (= 2^{k+1} - 2 + 1) = 2^{k+1} - 1$	Correct completion to $u_{k+1} = 2^{k+1} - 1$	A1
	Must see 4 things: $\underline{\text{true for } n = 1}$, $\underline{\text{assumption true for } n = k$, $\underline{\text{said true for } n = k + 1}$ and therefore $\underline{\text{true for all } n}$	Fully complete proof with no errors and comment. All the previous marks in (b) must have been scored.	Alcso
	Ignore any subsequent attempts e.g. <i>u</i>	$u_{k+2} = 2u_{k+1} + 1 = 2(2^{k+1} - 1) + 1$ etc.	(5)
			Total 7

Question Number	Scheme		Notes	Marks
8(a)	$det(\mathbf{A}) = 3 \times 0 - 2 \times 1 (= -2)$ Correct attempt at the determinant		M1	
	$det(\mathbf{A}) \neq 0$ (so A is non singular)	det(A) = -2 ar	nd some reference to zero	A1
	$\frac{1}{\det(\mathbf{A})}$	scores M0		(2)
(b)	$\mathbf{B}\mathbf{A}^2 = \mathbf{A} \Rightarrow \mathbf{B}\mathbf{A} = \mathbf{I} \Rightarrow \mathbf{B} = \mathbf{A}^{-1}$	Recognising t	hat A ⁻¹ is required	M1
	1(3-1)		rect terms in $\begin{pmatrix} 3 & -1 \\ -2 & 0 \end{pmatrix}$	M1
	$\mathbf{B} = -\frac{1}{2} \begin{pmatrix} 3 & -1 \\ -2 & 0 \end{pmatrix}$	$\frac{1}{\text{their det}(A)} \left($		B1ft
		Fully correct a		A1 (4)
	Ignore poor matrix algebra i	er only score 4/4		Total 6
(b) Way 2	$\mathbf{A}^2 = \begin{pmatrix} 2 & 3 \\ 6 & 11 \end{pmatrix}$	iotation if the	Correct matrix	B1
	$ \begin{pmatrix} a & b \\ c & d \end{pmatrix} \begin{pmatrix} 2 & 3 \\ 6 & 11 \end{pmatrix} = \begin{pmatrix} 0 & 1 \\ 2 & 3 \end{pmatrix} \Rightarrow \begin{cases} 2a + 6b = 0 \\ 3a + 11b = 1 \end{cases} o $	2c + 6d = 2 $3c + 11d = 3$	2 equations in a and b or 2 equations in c and d	M1
	$a = -\frac{3}{2}, b = \frac{1}{2}, c = 1, d = 0$		M1 Solves for a and b or c and d	M1A1
			A1 All 4 values correct	
(b) Way 3	$\mathbf{A}^2 = \begin{pmatrix} 2 & 3 \\ 6 & 11 \end{pmatrix}$		Correct matrix	B1
	$\left(\mathbf{A}^{2}\right)^{-1} = \frac{1}{"2" \times "11" - "3" \times "6"} \begin{pmatrix} "11" & "-3" \\ "-6" & "2" \end{pmatrix}$	see note	Attempt inverse of \mathbf{A}^2	M1
	$\mathbf{A}(\mathbf{A}^2)^{-1} = \frac{1}{4} \begin{pmatrix} 0 & 1 \\ 2 & 3 \end{pmatrix} \begin{pmatrix} 11 & -3 \\ -6 & 2 \end{pmatrix} or \frac{1}{4} \begin{pmatrix} 11 \\ -6 \end{pmatrix}$	$\begin{array}{c} -3 \\ 2 \end{array} \begin{pmatrix} 0 & 1 \\ 2 & 3 \end{pmatrix}$	Attempts $\mathbf{A}(\mathbf{A}^2)^{-1} or(\mathbf{A}^2)^{-1} \mathbf{A}$	M1
	$\mathbf{B} = -\frac{1}{2} \begin{pmatrix} 3 & -1 \\ -2 & 0 \end{pmatrix}$		Fully correct answer	A1
(1) 111 4			D 11 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	D.1
(b) Way 4	$\mathbf{BA} = \mathbf{I}$	2d = 0	Recognising that $BA = I$	B1
	$ \begin{vmatrix} a & b \\ c & d \end{vmatrix} \begin{vmatrix} 0 & 1 \\ 2 & 3 \end{vmatrix} = \begin{vmatrix} 1 & 0 \\ 0 & 1 \end{vmatrix} \Rightarrow \begin{vmatrix} 2b-1 \\ a+3b=0 \end{vmatrix} or $	c + 3d = 1	2 equations in a and b or 2 equations in c and d	M1
	$ \begin{pmatrix} a & b \\ c & d \end{pmatrix} \begin{pmatrix} 0 & 1 \\ 2 & 3 \end{pmatrix} = \begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix} \Rightarrow \begin{cases} 2b = 1 \\ a + 3b = 0 \end{cases} $ or $ a = -\frac{3}{2}, b = \frac{1}{2}, c = 1, d = 0 $		M1 Solves for a and b or c and d	M1A1
			A1 All 4 values correct	

Question Number	Scheme	Notes	Marks	
9 (a)	$y = 9x^{-1} \Rightarrow \frac{\mathrm{d}y}{\mathrm{d}x} = -9x^{-2}$	$\frac{\mathrm{d}y}{\mathrm{d}x} = k x^{-2}$		
	$xy = 9 \Rightarrow x \frac{\mathrm{d}y}{\mathrm{d}x} + y = 0$	Correct use of product rule. The sum of two terms, one of which is correct.	M1	
	or $\frac{dy}{dx} = \frac{dy}{dt} \cdot \frac{dt}{dx} = \frac{-3}{p^2} \cdot \frac{1}{3}$	their $\frac{dy}{dt} \times \left(\frac{1}{\text{their } \frac{dx}{dt}} \right)$		
	$\frac{dy}{dx} = -9x^{-2} \text{ or } x \frac{dy}{dx} + y = 0 \text{ or } \frac{dy}{dx} = \frac{-3}{p^2} \cdot \frac{1}{3}$	Correct differentiation.	A1	
	3 1	Applies $y - \frac{3}{p} = (\text{their } m)(x - 3p) \text{ or } y = (\text{their } m)x + c \text{ using}$		
	$y - \frac{3}{p} = -\frac{1}{p^2}(x - 3p)$	$x = 3p$ and $y = \frac{3}{p}$ in an attempt to find c.	M1	
		Their m must be a function of p and come from their dy/dx.		
	$x + p^2 y = 6p *$	Cso **given answer**	A1	
	Special case – if the correct gradient is <u>quoted</u> could score M0A0M1A1			
(b)	$x + q^2 y = 6q$	Allow this to score here or in (c)	B1	
(c)	$6p - p^2 y = 6q - q^2 y$	Attempt to obtain an equation in one	(1) M1	
	$y(q^{2} - p^{2}) = 6(q - p) \Rightarrow y = \frac{6(q - p)}{q^{2} - p^{2}}$ $x(q^{2} - p^{2}) = 6pq(q - p) \Rightarrow x = \frac{6pq(q - p)}{q^{2} - p^{2}}$	Attempt to isolate x or y – must reach x or $y = f(p, q)$ or $f(p)$ or $f(q)$	M1	
	$y = \frac{6}{p+q}$	One correct simplified coordinate	A1	
	$x = \frac{6pq}{p+q}$	Both coordinates correct and simplified	A1	
			(4)	
			Total 9	

Extra Notes

6(a) To show equivalence between $\frac{1}{4}k^2(k+1)^2 + (k+1)^3$ and $\frac{1}{4}(k+1)^2(k+2)^2$

$$\frac{1}{4}k^{2}(k+1)^{2} + (k+1)^{3} = \frac{1}{4}k^{4} + \frac{3}{2}k^{3} + \frac{13}{4}k^{2} + 3k + 1$$

Attempt to expand one correct expression up to a quartic

$$\frac{1}{4}(k+1)^2(k+2)^2 = \frac{1}{4}k^4 + \frac{3}{2}k^3 + \frac{13}{4}k^2 + 3k + 1$$

M1

Attempt to expand both correct expressions up to a quartic M1

One expansion completely correct (dependent on both M's)

A1

Both expansions correct and conclusion A1

Or

To show
$$\frac{1}{4}(k+1)^2(k+2)^2 - \frac{1}{4}k^2(k+1)^2 = (k+1)^3$$

$$\frac{1}{4}(k+1)^2(k+2)^2 - \frac{1}{4}k^2(k+1)^2$$
Attempt to subtract

$$\frac{1}{4}(k+1)^2(k+2)^2 - \frac{1}{4}k^2(k+1)^2 = k^3 + 3k^2 + 3k + 1$$
Obtains a cubic expression
A1
$$\frac{1}{4}(k+1)^2(k+2)^2 - \frac{1}{4}k^2(k+1)^2 = (k+1)^3$$
Correct expression
A1
$$\frac{1}{4}(k+1)^2(k+2)^2 - \frac{1}{4}k^2(k+1)^2 = (k+1)^3$$
Correct completion and comment
A1

8(b) Way 3

Attempting inverse of A^2 needs to be recognisable as an attempt at an inverse

E.g
$$(\mathbf{A}^2)^{-1} = \frac{1}{Their Det(\mathbf{A}^2)} (A changed \mathbf{A}^2)$$

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